## Maths $\%$ Stats UWI Cave Hill



The Discipline of Mathematics celebrates the International Day of Mathematics

Solve any of the three $\pi$-day puzzles below and send your solution to MathsStatsUWICaveHill@gmail.com the fastest solution to each puzzle wins $\$ 50$.

## Cross Number

Use the given clues to fill in this Cross Number puzzle. Remember, no entry in the grid may begin with " 0 ". Arithmetic sequences have a common difference, such as $2,5,8$, or $9,7,5$.

| 1 | 2 | 3 |  |  |
| :--- | :--- | :--- | :--- | :--- |
| 4 |  |  |  | 5 |
| 6 |  |  | 7 |  |
|  |  | 8 |  |  |
|  |  |  |  |  |


|  | Clues Across |
| :--- | :--- |
| 1 | A prime number |
| 4 | 100 less than 2-Down |
| 6 | Perfect cube |
| 8 | No clue needed! |
| 9 | Perfect cube |
|  |  |
| 1 | Clues Down |
| 2 | Product of the digits of 6-Across |
| 3 | Odd digits whose sum is over 40 |
| 5 | Factor of the reverse of 6-Across |
| 7 | Digits form an arithmetic sequence |

## Seven Circles in a Dodecagon



In the figure on the left, a regular dodecagon (a polygon with 12 equal sides) is circumscribed by a large circle (the vertices of the dodecagon are shown as •). Inside the dodecagon are seven circles (in green), all of the same radius, that are tangential to each other and/or the dodecagon, the points of tangency are shown as $\diamond$.

What is the proportion of the area of these seven small circles (in green) to the area of the large (circumscribing) circle?

## Sudoku

Fill in the cells so that each row, column, and $3 \times 3$ square contains each of the numbers $1,2, \ldots, 9 . A \nabla$ (in red) between cells means the product of those entries is greater than 23. A $\triangle$ (in blue) means the product is less than 23 . In addition, a 2 or 3 appears inside whenever the difference of those entries (in some order) is 2 or 3 , respectively. Note that this means if there is no number, then those entries are not 2 or 3 apart from each other.


